ADVANCED ALGEBRA & TRIG CORE AND HONORS SUMMER WORK

**THE WORK SHOWN IN THIS PACKET IS ONE METHOD. PLEASE USE ANOTHER METHOD IF IT IS MORE COMFORTABLE FOR YOU.

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Directions: The concepts covered in this packet are skills that students should have mastered in your previous Algebra course. If you are drawing a blank, please refer to the problems that have already been completed for you.

Rationale: The math course you are starting in the fall has some high expectations. It is assumed you can...

- (1) follow order of operations appropriately in all situations
- (2) solve a variety of linear, absolute value, & quadratic equations and some inequalities
- (3) graph basic linear functions
- (4) factor, factor, factor
- (5) simplify square roots/radicals
- (6) follow the rules of exponents
- (7) use and understand basic function notation

To refresh on these topics, you'll need to practice these skills in the weeks leading up to the beginning of the 2021-22 school year.

Resources: For each even numbered problem you need to complete, there is an odd-numbered example problem worked out in detail. If that's not enough to guide your work, then we suggest you google the topic you are struggling with or go to one of the following websites & search the topic...

https://www.desmos.com

https://www.khanacademy.org/

http://www.purplemath.com/

http://www.mathgoodies.com/students.html

Requirement: A requirement of this course is that you purchase a graphing calculator. Although these can be expensive, we will use it in every chapter to supplement the content that is being learned. Below are *suggested* calculators that are appropriate to use in Advanced Algebra Honors and can be used in subsequent years through college level math courses.

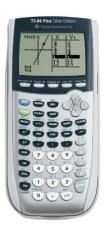
TI - 83 +

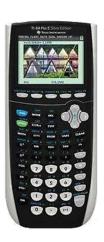


If you purchase a TI - 83, it needs to be a plus (+) model. You will need the blue/purple "APPS" key.

This is the button we are looking for.

TI - 84/TI - 84+







These calculators come in various models, as they have been updated over the years. ANY TI - 84 is appropriate. It can be a plus (+) model, a C or CE model or a silver edition model. It can also have a black and white screen or a color screen. The most efficient calculators are the newest thinner calculators with a color screen.

It is highly recommended to purchase one of these calculators as soon as possible, as they do sell out quickly at the beginning of the school year. These versions of TI calculators are what will be used in class. It is not recommended that you buy a device that is not listed here.

Thank you,

Mr. Strzelczyk (Honors and Core)

Mrs. Zwart (Honors)

Mrs. Coletta (Core)

(Willowbrook - Advanced Algebra & Trig Honors AND Core teachers 2021-22)

#1 - 10: Evaluate showing work. (No Calculator)

1.
$$4+3 \cdot 4 \div 2-9$$

2.
$$18-12 \div 6 \bullet 2-10$$

4.
$$20 - (7 + (-9))^2 \cdot 3$$

5.
$$(2x)^2 - y$$
 when $x = 3$, $y = 17$

6.
$$3x - 4y^3$$
 when $x = 7$, $y = -1$

7.
$$\frac{1}{2}(x-7)-3x$$
 when $x=-11$

$$\frac{\frac{1}{2}(-11-1)-3(-11)}{\frac{1}{2}(-18)-3(-11)}$$

$$-9+33$$

$$\boxed{24}$$

8.
$$b^2 - 4ac$$
 when $a = 2$, $b = -3$, $c = -1$

9.
$$\frac{3b-a}{b+a}$$
 when $a = 3$, $b = -4$

10.
$$\frac{4b+2a}{2b}$$
 when $a = 3$, $b = -4$

#11 - 18: Simplify each expression showing work. (No Calculator)

11.
$$x - x^2 + 3x^2 + 5x$$

$$\frac{-x^{2}+x}{+3x^{2}+5x}$$

$$\frac{-x^{2}+5x}{2x^{2}+6x}$$

12.
$$4x^2 - 3x + 5x - 6x^2$$

13.
$$6y(-2)3y(-8) + 2y$$

14.
$$5m-3m(m+2)+5m^2$$

15.
$$(4+x)(x-3)$$

16.
$$(3x-4)(2x+1)$$

17.
$$(2+3x)^2$$
 **write it out $(2+3x)(2+3x)$, $(2+3x)(2+3x)$,

18.
$$(2x-5)^2$$

#19 - 40: Solve each equation showing algebraic work. (No Calculator)

19.
$$4x-3=9$$
+3 +3

 $4x=12$

20.
$$3-5x=16$$

21.
$$\frac{3x-6=5x+12}{-3x-12-3x-12}$$

$$\frac{-18:2x}{2}$$

22.
$$16 - 8x = 4x + 6$$

23.
$$-3(2x+5)=20$$

$$-6x - 15 = 20$$

$$+15 + 15$$

$$-6x = 35$$

24.
$$4(3x-7) = -40$$

Simplified * Improper fractions are okay!

25.
$$2(4-x)=16+2x$$

$$\frac{8 - 2x = 16 + 2x}{-16 + 2x} = \frac{16 + 2x}{4}$$

27.
$$4-3(4x+6)=1$$

$$4-3(4x+6)=1$$

$$4-12x-18=1$$

$$-12x-14=1$$

$$+14=14$$

$$-12x=15$$

$$-12=12$$

$$x=-4 \quad \{-5\}$$

29.
$$5(3x-2)+10=2(5-6x)$$

31.
$$(\frac{2}{3}m+5=\frac{2}{5}m-9)$$
 an Equation 32. $4-\frac{5}{6}x=\frac{1}{2}x+2$

fractions

$$\frac{4m = -210}{4}$$

$$m = \frac{105}{2} \left\{ \frac{-105}{2} \right\}$$

33. Solve for
$$b_1 : \mathbf{Z} - A = \frac{h(b_1 + b_2)}{2} \cdot \mathbf{Z}$$

$$\frac{2A = h(b_1 + b_2)}{h}$$

$$\frac{2A}{h} = b_1 + b_2$$

$$-b_2$$

$$b_1 = \frac{2A}{h} - b_2$$

26.
$$5x-20=6(2x+1)$$

28.
$$18 = 10 - 2(2x + 3)$$

30.
$$20+8(3+4x)=-3(6x-5)$$

$$32. \quad 4 - \frac{5}{6}x = \frac{1}{2}x + 2$$

34. Solve for h:
$$A = \frac{h(b_1 + b_2)}{2}$$

37.
$$|3-2x|=13$$

$$3-2x=13 \text{ or } 3-2x=-13$$
 $-2x=10$
 $-2x=-16$
 $x=-5$
 $x=8$
 $x=-5,8$

39.
$$4|2x-1|+2=22$$

$$\frac{4|2x-1| = \frac{20}{4}}{|2x-1| = 5}$$

$$0 = \frac{2x-1}{2x-1} = \frac{5}{4}$$

41.
$$3+2|x-6|=13$$

38.
$$22 = |5 - 4x|$$

40.
$$\frac{2}{3}|x-8|-5=11$$

42.
$$-2|2x+5|-6=22$$

#43-52: Solve and graph on a number line. No Calculator.

43.
$$2x+5 \le -9$$

$$-5 -5$$

$$2x \le -14$$

$$x \le -7$$

$$\le \text{ or } \ge \text{ closed point}$$

$$0 > 0 > 0 > 0 > 0$$

$$0 > 0 > 0 > 0$$

$$0 > 0 > 0 > 0$$

44.
$$4+3x \ge 19$$

(4.1.9 O)

45.
$$3-x<6$$

$$-x<3$$

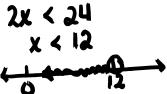
$$-x<3$$

$$-1$$
then the $4/3$

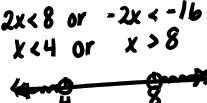
$$x>-3$$
 flips.

46.
$$2-3x \ge 14$$

47. 5x-6 < 3x+18



- 51. 4 + 2x < 12 or 5 2x < -11



48. 3x+5>6x-12

50. 19 > 5 - 2x > -7

52. $3-6x > 15 \text{ or } 5x-3 \ge 12$

#53-64: The following questions are all about lines on the coordinate plane. No Calculator.

- 53. Find the slope between (3,4) & (-2,5)
- 54. Find the slope between (-6,7) & (3,-5)

- 55. Find the slope between (5,7) & (5,-9)
- 56. Find the slope between (-4,7) & (8,7)
- 57. Write the equation of the line in #55
- 58. Write the equation of the line in #56

(It is a vertical line)

- 59. Write in slope-intercept form: **y: mx+b** 3x - 2y = 4x - 7
- 60. Write in slope-intercept form: 4y - 6x = 5y - 12

#61-62: Determine the slope, then write the coordinates of the x-intercept and y-intercept of the line.

Slope

$$\frac{3x+2y=12}{2}$$
 $\frac{x+int}{3x+2(0)}$ $\frac{y-int}{y}$ $\frac{3x+2(0)}{2}$ $\frac{y-int}{3}$ $\frac{y-int}{3}$ $\frac{3x+2}{3}$ $\frac{3x+$

62.
$$4x - 6y = -20$$

#63-64: Determine the slope of the line parallel and the slope of the line perpendicular to the given line.

63.
$$3x-2y=6$$
-2y: $3x+6$
 $y: \frac{3}{2}x-3$
 $ml: \frac{3}{3}ml: \frac{2}{3}$

64.
$$5-7x-5y=7$$

#65-84: Factor each expression completely. No Calculator

65.
$$\frac{21xy}{7x} - \frac{14xz}{7x}$$
 GCF $7x (3y - 2z)$

66.
$$18a^3 + 4a^2$$

67.
$$\frac{4x^{2}y^{2}z + 6xz^{2}}{2x^{2}}$$

$$2x^{2}z + \frac{6xz^{2}}{2x^{2}}$$

$$2x^{2}z + 3z$$

$$68. \quad 24x^4y^5 - 8x^3y^7 + 4x^2y^8$$

69.
$$x^2+6x+8$$
 & Guess & Check 70. $x^2+11x+28$ (x44)(x+2) $x^2+4x+2x=8$

71.
$$x^2 - 8x + 12$$

 $(x - 6)(x - 2)$
 $4x^2 - 6x - 2x + 12$

72.
$$x^2 - 11x + 24$$

73.
$$x^2-6x-16$$
 $(x-8)(x+2)$
 $(x^2-8x+2x-16)$

74.
$$x^2 - 3x - 10$$

75.
$$2x^{2} + 7x + 3$$

 $(2x + 1)(x + 3)$
 $12x^{2} + 6x + x + 3$
77. $4x^{2} - x - 3$

76.
$$3x^2 + 7x + 2$$

$$(4x + 3)(x - 1)$$

$$\sqrt{4x^2 - 4x + 3x - 3}$$

78.
$$4x^2 + 5x - 6$$

79.
$$5x^2-125y^2$$
 ① GCF

 $5(x^2-25y^2)$ ② Difference of squares pattern

 $5(x-5y)(x+5y)$

80.
$$3h^2 - 27m^2$$

81.
$$4x^2-9$$
 (2x +3)(2x-3)

82.
$$81y^2 - 49$$

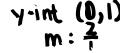
83.
$$4x^2-12x+9$$
 $(2x-3)(2x-3)$
 $(2x-3)^2$
When duplicate factors

84.
$$9x^2 - 30x + 25$$

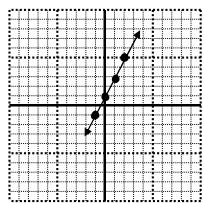
#85-94: Solve each quadratic equation showing algebraic work and exact answers (integers, simplified ratios, or simplified radicals). You may use any appropriate method. Suggested methods: factoring, square root method, or the quadratic formula. If you do not know the quadratic formula, then Google it please. We expect you to know the quadratic formula. No

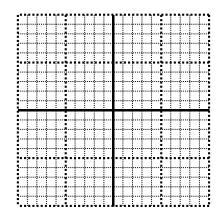
Calculator.

95.
$$y = 2x + 1$$



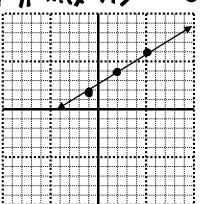
96.
$$y = -\frac{2}{3}x - 2$$

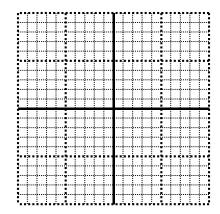




97.
$$y-2=\frac{2}{3}(x+1)$$
 Start pt (-1,2)
Pt. Slope y-y,= m(x-y,) m= $\frac{2}{3}$

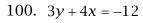
98.
$$y+3=-\frac{3}{4}(x-4)$$

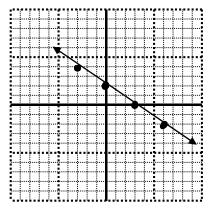


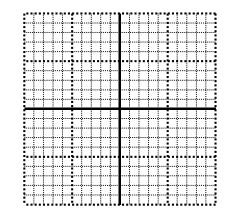


99.
$$2x+3y=6$$

 $3y: -\frac{2}{3}x+6$ $y: -\frac{2}{3}x+2$
 $y: int(0,2)$
 $m: \frac{2}{3}$

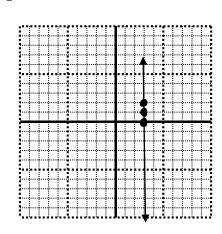




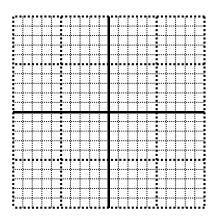


101.
$$x = 3$$

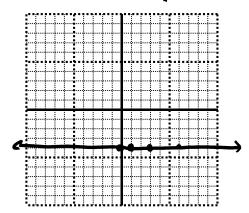
X	L
3	Ö
3	١
3	2



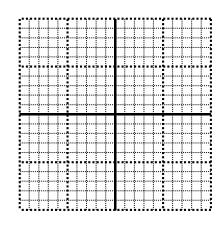
102.
$$x = -5$$



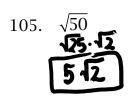
103.
$$y = -4$$
 * All coordinates have 4 as y



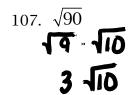
104. y = 7



#105 - 110: Simplify the square root. No Calculator.



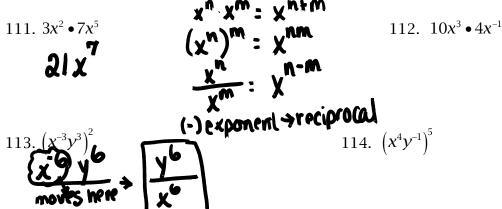
*Look for the largest perfect square that 106. $\sqrt{98}$ divides into 50.



108. $\sqrt{132}$

110. $\sqrt{675}$

#111-118: Use the properties/rules of exponents to simplify the expression. No Calculator.



115.
$$\frac{x^{7}y^{3}}{x^{5}y^{6}} \Rightarrow x^{7\cdot 5}y^{3\cdot 6} \xrightarrow{QR} \text{ batte in the homerator.}$$

$$\frac{x^{2}}{y^{3}} \xrightarrow{Y^{3}} y^{3} \xrightarrow{QR} \text{ batte in the homerator.}$$

$$y^{3}y^{4}y^{5}y^{6} \xrightarrow{y^{3}z^{6}} y^{2}z^{2}$$

$$y^{4}y^{5}y^{6}y^{6} \xrightarrow{y^{2}z^{6}} y^{2}z^{2}$$

$$y^{5}y^{6}y^{6} \xrightarrow{y^{2}z^{6}} y^{2}z^{6}$$

$$y^{5}y^{6}y^{6} \xrightarrow{y^{2}z^{6}} y^{2}z^{6}$$

$$y^{5}y^{6}y^{6} \xrightarrow{y^{2}z^{6}} y^{2}z^{6}$$

$$y^{5}y^{6}y^{6} \xrightarrow{y^{2}z^{6}} y^{2}z^{6}$$

$$y^{5}y^{6}y^{6} \xrightarrow{y^{6}z^{6}} y^{6}z^{6}$$

$$y^{6}y^{6}y^{6}y^{6} \xrightarrow{y^{6}z^{6}} y^{6}z^{6}$$

$$y^{6}y^{6}y^{6}y^{6}y^{6} \xrightarrow{y^{6}z^{6}} y^{6}z^{6}$$

$$y^{6}y^{6}y^{6}y^{6} \xrightarrow{y^{6}z^{6}} y^{6}z^{6}$$

$$y^{6}y^{6}y^{6}y^{6}y^{6} \xrightarrow{y^{6}z^{6}} y^{6}z^{6}$$

117.
$$\left(\frac{3a^4b^3}{c^7}\right)^{-2} \rightarrow \frac{3^2a^8b^6}{c^{14}}$$
 *All values move due 118. $\left(\frac{2a^4b^{-1}}{c^2}\right)^{-3}$ exponent

#119-126: Perform the given operations for the functions...

$$f(x) = 3x - 5$$
 $g(x) = -x^2 + 2x - 7$ and $h(x) = -2x + 1$

119.
$$2f(x)+3g(x)$$

 $2(3x-5)+3(-x^2+2x-7)$
 $6x-10-3x^2+6x-21$
 $-3x^2+12x-31$

121.
$$2h(x) - g(x)$$

$$2(-2x+1) - (-x^2+2x-7)$$

$$-4x+2+x^2-2x+7$$

$$x^2-6x+9$$
122. $4g(x)-3f(x)$

$$f(x) = 3x - 5$$
 $g(x) = -x^2 + 2x - 7$ and $h(x) = -2x + 1$

123.
$$f(x) \cdot g(x)$$
 * Distribute twice $(3x-5)(-x^2+2x-7)$ $-3x^3+6x^2-21x+5x^2-10x+35$ $-3x^3+11x^2-31x+35$

125. Evaluate:
$$f(-3)$$
: $3(-3)$ - 5

126. $f(-3)$: -9 - 5

127. $f(-3)$: -14

126. Evaluate: g(-5)

KEY to even answers

2. 4 4. 8 6. 25 8. 17 10.
$$\frac{5}{4}$$
 12. $-2x^2 + 2x$ 14. $2m^2 - m$

16.
$$6x^2 - 5x - 4$$
 18. $4x^2 - 20x + 25$ 20. $\left\{-\frac{13}{5}\right\}$ 22. $\left\{\frac{5}{6}\right\}$ 24. $\left\{-1\right\}$

26.
$$\left\{-\frac{26}{7}\right\}$$
 28. $\left\{-\frac{7}{2}\right\}$ 30. $\left\{-\frac{29}{50}\right\}$ 32. $\left\{\frac{3}{2}\right\}$ 34. $h = \frac{2A}{b_1 + b_2}$

36.
$$\{-6,18\}$$
 38. $\left\{-\frac{17}{4}, \frac{27}{4}\right\}$ 40. $\{-16, 32\}$ 42. No Solution

44.
$$x \ge 5$$
 46. $x \le -4$ 48. $x < \frac{17}{3}$ 50. $-7 < x < 6$

$$48. \ x < \frac{}{3}$$

50.
$$-7 < x < 6$$

$$\underbrace{\frac{17}{3}}$$

52.
$$x < -2$$
 or $x \ge 3$ 54. $-\frac{4}{3}$

54.
$$-\frac{4}{3}$$

58.
$$y = 7$$

56. 0 58.
$$y = 7$$
 60. $y = -6x + 12$

62.
$$m = \frac{2}{3} x - \text{int} = (-5,0) y - \text{int} = \left(0, \frac{10}{3}\right)$$
 64. $m \parallel = -\frac{7}{5} \quad m \perp = \frac{5}{7}$

64.
$$m \parallel = -\frac{7}{5}$$
 $m \perp = \frac{5}{7}$

66.
$$2a^2(9a+2)$$
 68. $4x^2y^5(6x^2-2xy^2+y^3)$ 70. $(x+7)(x+4)$

70.
$$(x+7)(x+4)$$

72.

$$(x-8)(x-3)$$

74.
$$(x-5)(x+2)$$
 76. $(3x+1)(x+2)$ 78. $(4x-3)(x+2)$ 80. $3(h+3m)(h-3m)$

78.
$$(4x-3)(x+2)$$

80.
$$3(h+3m)(h-3m)$$

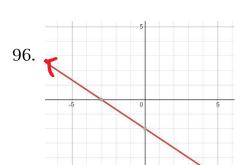
82.
$$(9y+7)(9y-7)$$
 84. $(3x-5)^2$ 86. $\{-11,6\}$ 88. $\left\{\frac{2}{3},\frac{3}{2}\right\}$

84.
$$(3x-5)^2$$

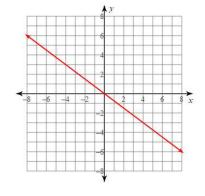
88.
$$\left\{\frac{2}{3}, \frac{3}{2}\right\}$$

92.
$$\{\pm 3\sqrt{5}\}$$

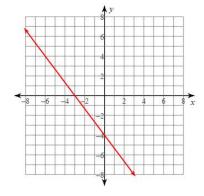
90.
$$\{-1,2\}$$
 92. $\{\pm 3\sqrt{5}\}$ 94. $\{2\pm \frac{\sqrt{14}}{2}\}$



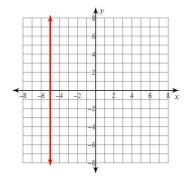




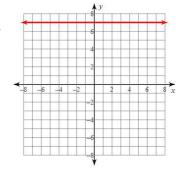
100.



102.



104.



106. $7\sqrt{2}$

108.
$$2\sqrt{33}$$

110.
$$15\sqrt{3}$$

110.
$$15\sqrt{3}$$
 112. $40x^2$

114.
$$\frac{x^{20}}{y^5}$$

116. y^2z^4

118.
$$\frac{b^3c^6}{8a^{12}}$$

120.
$$-x^2 - 2x - 5$$

122.
$$-4x^2 - x - 13$$

120.
$$-x^2 - 2x - 5$$
 122. $-4x^2 - x - 13$ 124. $-6x^2 + 13x - 5$